# **Visual Based Control System for a Tentacle Manipulator**

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**Abstract**: The control problem of a tentacle manipulator by using a robust 3 D visual servoing is presented. The theoretical model of this class of arms is studied. Servoing is based on binocular vision obtained by two cameras that ensure a continuous measure of the arm parameters. The control errors function is built in 3D cartesian space by the visual information obtained in the two image planes. The 2D errors are determined as the shape errors, they are calculated on the differences between the actual and desired continuous angle values. A spatial error is determined and a control law is discussed. The stability of the closed-loop control system is proven. Computer simulations and real 3-D experiments are presented to show the applicability of the method.

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## **1.Introduction**

An ideal tentacle manipulator is a non-conventional robotic arm with an infinite mobility. It has the capability to take sophisticated shapes and to achieve any position and orientation in a 3D space. These systems are also known as hyperredundant manipulators and, over the past several years, there has been a rapidly expanding interest in the study and construction of them. The control of these systems is very complicated and a great number of researchers tried to offer solutions for this difficult problem. In [1] it was analysed the control by cables or tendons meant to transmit forces to the elements of the arm in order to closely approximate the arm as a truly continuous backbone. Also, Mochiyama has investigated the problem of controlling the shape of an HDOF rigid-link robot with two-degree-of-freedom joints using spatial curves [7], [8]. Important results were obtained by Chirikjian and Burdick [3] – [6] that laid the foundations for the kinematic theory of hyperredundant robots. Their results are based on a "backbone curve" that captures the robot's macroscopic geometric features. The inverse kinematic problem is reduced to determining the time varying backbone curve behaviour. New methods for determining "optimal" hyper-redundant manipulator configurations based on a continuous formulation of kinematics are developed. In [2], Gravagne analysed the kinematic model of "hyper-redundant" robots, known as



**Figure 1.** 

**Figure 2.** 

"continuum" robots. Robinson and Davies [8] present the "state of art" of continuum robots, outline their areas of application and introduce some control issues. The great number of parameters, theoretically an infinite number, makes very difficult the use of classical control methods and the conventional transducers for position and orientation.

In this paper the method of image-based servoing [12,15] for a hyperredundant arm is studied. Servoing is based on binocular vision, a continuous measure of the arm parameters derrived from the real-time computation of the binocular optical flow over the two images, is compared with the desired position of the arm. The control error function is built in 3D cartesian space by the visual information obtained by two cameras in two image planes [13]. The two 2D errors obtained in the two image planes are determined by the two differences between the actual and desired continuous angle values that define the projections of the arm shape. The plane errors can be considered as the errors of the arm shape. These errors are used to calculate the spatial error and a control law is synthesized.

For the closed-loop control system and a control law the stability is proven by using the Lyapunov second method. The error function is computed in the image spaces virtually and no calibration (camera parameters) is required allowing the synthesis of more robust control laws.

The paper is organised as follows: Section II reviews the basic principles of a hyperredundant manipulator; Section III presents the camera video system; Section IV introduces the servoing system; Section V verifies by computer simulations the control law and Section VI presents the results of the method for a real 3D application.

## **2. Background**

Consider a 3D hyperredundant robot with a three dimensional Cartesian coordinate frame called the robot coordinate frame whose axes are labeled X, Y, Z. The mechanical structure represents an ideal arm, with an uniform distributed mass and torque, with ideal flexibility that can take any arbitrary shape (Fig. 1). We will neglect friction and structure damping. The essence of the model is a  $3 -$  dimensional backbone curve C that is parametrically described by a vector  $r(s) \in \mathbb{R}^3$  and an associate frame  $\Phi(s) \in \mathbb{R}^3$  whose columns create the frame base (Fig. 2) [2,3]. The independent parameter s is related to the arc length from the origin of the curve C. The position of a point s on the curve C is defined by the position vector,

$$
\bar{\mathbf{r}} = \bar{\mathbf{r}}(\mathbf{s}) \tag{2.1}
$$

where  $s \in [0,1]$ . For a dynamic motion, the time variable is introduced,  $\overline{r} = \overline{r}(s, t)$ . The parametrisation of the curve C is based upon two "continous angle"  $\theta(s)$  and q(s) [3,5] (Fig. 2). At each point  $\overline{r}(s, t)$ , the robot's orientation is given by a right-handed orthonormal basis vector  $\{e_x, e_y, e_z\}$  and its origin coincides with the point  $\overline{r}(s,t)$ . The set of backbone frames can be parametrized as

$$
\Phi^s(t) = \left(\mathbf{e}_x(s,t), \mathbf{e}_y(s,t), \mathbf{e}_z(s,t)\right) \tag{2.2}
$$

The pointer vector on curve C is given by  
\n
$$
\vec{r}(s, t) = (x(s, t), y(s, t), z(s, t))^{T}
$$
\nwhere  
\n
$$
x(s, t) = \int_{0}^{s} \sin \theta(s', t) \cdot \cos q(s', t) \cdot ds'
$$
\n
$$
y(s, t) = \int_{0}^{s} \cos \theta(s', t) \cdot \cos q(s', t) \cdot ds'
$$
\n
$$
z(s, t) = \int_{0}^{s} \sin q(s', t) \cdot ds'
$$
\n(2.4)

where  $s' \in [0, s]$ .

We adopt the following interpretation [6,7]: at any point s the relation (2.4) determines the current position and  $\Phi^s$  determines the robot's orientation and the robot's shape is defined by the behaviour of function  $\theta(s)$  and q(s). The robot "grows" from the origin by integrating to get  $\overline{r}(s,t)$ ,  $s \in [0,1]$ . By using this definition, two position of the hyperredundant can be defined by a curve C as

$$
C: (\theta(s), q(s)) \qquad , s \in [0,1] \qquad (2,5)
$$

The motion and orientation of the arm are given by the distributed forces on the legth of the arm,  $F_0(s, t)$ and  $F_q(s, t)$  that rotate the element ds in the planes of the angles  $\theta(s)$  and  $q(s)$ , respectively. The

manipulator model is considered as a distributed parameter system defined on a fixed spatial domain [0,l] and the spatial coordinate is s. The dynamic model of this manipulator with hyperredundant configuration can be obtained from Hamilton partial differential equations [10].

$$
\frac{\partial \omega(t,s)}{\partial t} = \frac{\delta H}{\delta v(t,s)}
$$
\n
$$
\frac{\partial v(t,s)}{\partial t} = -\frac{\delta H}{\delta \omega(t,s)} + F(t,s)
$$
\n(2.6)

where  $\omega$  and  $v$  are the generalised coordinates and momentum derivated respectively and  $\delta(.)/\delta(.)$ denotes a functional partial derivative.

The state of the system ot any fixed time t is specified by the set  $(\omega(t,s), v(t,s))$ , where  $\omega \in [\theta \ q]^T$  The control force is a distributed force along the arm

$$
\mathbf{F} = \begin{bmatrix} \mathbf{F}_{\theta} & \mathbf{F}_{\mathbf{q}} \end{bmatrix}^{\mathrm{T}} \tag{2.7}
$$

In the Appendix 1 the dynamic model of the 3D spatial hyperredundant arm is determinated.

#### **3. Camera System**



Two video cameras provide two images of the whole robot workspace. The two images planes are parallel with XOY and ZOY planes from robot coordinate frame, respectively (Fig. 3). The cameras provide the images of the scene that stored in the frame grabber's video memory being displayed on the computer screens. Related to the image planes are defined two dimensional coordinate frames, called screen

coordinate frames or image coordinate systems. Denote  $X_{S_1}$ ,  $Y_{S_1}$  and  $Z_{S_2}$ ,  $Y_{S_2}$ , respectively, the axes of the two screen coordinate frames provided by the two cameras. The spatial centers for each camera are located at the distances D1 and D2, with respect to the XOY and ZOY planes, respectively. The orientation of the cameras arround the optical axes with respect to the robot coordinate frame, are noted by  $\psi$  and  $\varphi$ , respectively. A point P in the coordinate frame is

$$
P=[x, y, z]^T
$$
 (3.1)

The description of a point P in the two screen coordinate frames are denoted by

$$
P_{S_1} = [x_{S_1}, y_{S_1}] \tag{3.2}
$$

$$
P_{S2} = [z_{S_2}, y_{S_2}] \tag{3.3}
$$

Geometric optics are used to model the mapping between the robot Cartesian space and the screen coordinate systems. We assume that the quantization and the lens distortion effects are negligible. The description of the point  $P=[x, y, z]^T$  in the robot coordinate frame is given in terms of screen coordinate frames as [9]

$$
\begin{bmatrix} x_{s_1} \\ y_{s_1} \end{bmatrix} = \alpha_1 \cdot \frac{\lambda_1}{\lambda_1 - (D_1 + x)} \cdot R(\phi) \cdot \begin{bmatrix} x \\ y \end{bmatrix} - \begin{bmatrix} o_{11} \\ o_{12} \end{bmatrix} + \begin{bmatrix} c_{x_1} \\ c_{y_1} \end{bmatrix}
$$
(3.4)

for the  $Z_{S_1}O_{S_1}Y_{S_1}$  frame and

$$
\begin{bmatrix} z_{s_2} \\ y_{s_2} \end{bmatrix} = \alpha_2 \cdot \frac{\lambda_2}{\lambda_2 - (D_2 + x)} \cdot R(\phi) \cdot \begin{bmatrix} z \\ y \end{bmatrix} - \begin{bmatrix} o_{21} \\ o_{22} \end{bmatrix} + \begin{bmatrix} c_{z_2} \\ c_{y2} \end{bmatrix}
$$
\n(3.5)

for the  $Z_{S_2}O_{S_2}Y_{S_2}$  frame, where  $[c_{x_1}, c_{y_1}]^T$  and  $[c_{z_2}, c_{y_2}]^T$  the image centers,  $\alpha_1$  and  $\alpha_2$  are the scale factors of the length units in the front image planes given in pixel/m [9,15],  $R(\psi)$  and  $R(\varphi)$  are the rotation matrices generated by clockwise rotating the cameras about their optical axes by  $\psi$  and  $\varphi$ radians, respectively, and  $[o_{11}, o_{12}]^T$  and  $[o_{21}, o_{22}]^T$  represent the distances between the optical axes and the XOY and ZOY planes, respectively.

In Fig. 4 are presented the screen images of the two cameras. From the relations (3.4), (3.5), we obtain



**Figure 3** 

$$
\begin{bmatrix}\n\Delta x_{s_1} \\
\Delta y_{s_1}\n\end{bmatrix} = \alpha_1 \cdot \frac{\lambda_1}{\lambda_1 - (D_1 + x)} \cdot \begin{bmatrix}\n\Delta x \\
\Delta y\n\end{bmatrix}
$$
\n(3.6)\n
$$
\begin{bmatrix}\n\Delta z_{s_2} \\
\Delta x\n\end{bmatrix} = \alpha_2 \cdot \frac{\lambda_2}{\lambda_1 - (D_1 + x)} \cdot \begin{bmatrix}\n\Delta z \\
\Delta z\n\end{bmatrix}
$$
\n(3.7)

 $\left[\alpha_2 \cdot \frac{\lambda_2}{\lambda_2 - (D_2 + x)} \cdot \begin{bmatrix} \Delta z \\ \Delta y \end{bmatrix}\right]$  $\frac{1}{2}$  $\left[\Delta y_{s_2}\right] = \alpha_2 \cdot \frac{\lambda_2}{\lambda_2 - (D_2 + x)} \cdot \left[\Delta y\right]$  $\begin{bmatrix} s_2 \\ s_2 \end{bmatrix}$  =  $\alpha_2 \cdot \frac{\lambda_2}{\lambda_2 - (D)}$ 

and the orientation angles for each plane will be

$$
tg\theta_s = \frac{\Delta x_{s_1}}{\Delta y_{s_1}} = \frac{\Delta x}{\Delta y} = tg\theta
$$
\n(3.8)

hence

$$
\theta_s(s') = \theta(s) \quad , s \in [0, l], s' \in [0, l']
$$
\n
$$
\text{for the plane } \mathbb{Z} \quad \text{O} \quad \mathbb{Y} \quad \text{and} \tag{3.9}
$$

for the plane  $Z_{S_1} O_{S_1} Y_{S_1}$  and

$$
tgq_s = \frac{\Delta z_{s_2}}{\Delta y_{s2}} = \frac{\Delta z}{\Delta y}
$$

This relation allows the computation of the orientation angle  $q_s$  in the plane  $Z_{S_2}O_{S_2}Y_{S_2}$ 

$$
tgq_s(s'') = tgq(s) \cdot \frac{1}{\cos \theta(s)}, s \in [0,1], s'' \in [0,1'']
$$
\n(3.10)

where, s',s'' and  $\vert$ ',  $\vert$ '' represent the projections of the variable s and the length 1 in the two planes, respectively. The projection of the forces on the two planes can be easily inferred from the Fig. 2 and the relations (3.8)-(3.10),

$$
F_{\theta_{\rm S}} = F_{\theta} \tag{3.11}
$$

$$
F_{q_s} = F_q \cdot \sqrt{\cos^2 q + \sin^2 q \cdot \cos^2 \theta} \tag{3.12}
$$

## **4. Servoing System**

The control system is an image – based visual servo control where the error control signal is defined directly in terms of image feature parameters. The desired position of the arm in the robot space is defined by the curve  $C^d$ ,

$$
C: (\theta^d(s), q^d(s)) , s \in [0,1]
$$
\n
$$
(4.1)
$$

or, in the two image coordinate frames  $Z_{S_1} O_{S_1} Y_{S_1}$  and  $Z_{S_2} O_{S_2} Y_{S_2}$ , by the projection of the curve C,

$$
C_{s_1}^d: (\theta_s^d(s')) \qquad , s' \in [0,1'] \qquad (4.2)
$$

$$
C_{s_2}^d : (q_s^d(s'')) \qquad, s'' \in [0, l''] \tag{4.3}
$$

Define the motion errors as

$$
e_{\theta}(t,s) = \theta(t,s) - \theta_{d}(s) \qquad , s \in [0,1]
$$
\n
$$
(4.4)
$$



**Figure 5** 

$$
e_q(t,s) = q(t,s) - q_d(s)
$$
,  $s \in [0,1]$  (4.5)

or, in the image coordinate frames, by

$$
e_{\theta_S}(t,s') = \theta_S(t,s') - \theta_s^d(s')
$$
  $s' \in [0,1']$  (4.6)

$$
e_{q_s}(t, s'') = q_s(t, s'') - q_s^d(s'')
$$
  $s'' \in [0, l'']$  (4.7)

The global control system is presented in Fig. 5.

The control problem of this system is a direct visual servocontrol but we do not use the clasical concept of the position control in which is minimized the error between the robot end-effector and target. In this paper we will use the control of the shape of the curve in each point of the mechanical structure. The method is based on the particular structure of the system defined as a "backbone with two continuous angles  $\theta(s)$  and  $q(s)$ ". The control of the system is based on the control of the two angles  $\theta(s)$  and  $q(s)$ . These angles are measured directly or indirectly. The angle  $\theta(s)$  is measured directly by the projection on the image plane  $Z_{S_1}O_{S_1}Y_{S_1}$  (relation 3.9) and q(s) is computed from the projection on the image plane  $Z_{S_2}$  *O<sub>S</sub>*,  $Y_{S_2}$  (relation 3.10). The stability of the closed-loop system is proven by the Lyapunov's second method but, in order to avoid the complex problems derived by using the nonlinear derivation integral model, in this paper will be developed a method based on the energy-work relationship [14].

**Propostion** The closed-loop hyperredundant arm system is stable if the control law is given by

 $\bullet$ 

$$
F_{\theta}(s,t) = -k_{\theta}^{1}(s) \cdot e_{\theta_{s}}(s',t) - k_{\theta}^{2}(s) \cdot e_{\theta_{s}}(s',t)
$$
\n(4.8)

$$
F_q(s,t) = -k_q^1(s) \cdot \left[ tg^{-1}(\cos \theta_s(s',t)) \cdot tgq_s(s'',t) - q^d(s) \right] \tag{4.9}
$$

where  $s' \in [0, l']$ ,  $s'' \in [0, l'']$  and  $k_{\theta}^{1}(s), k_{\theta}^{2}(s), k_{q}^{1}(s)$  are positive coefficients of the control law for all  $s \in [0,1]$ . Proof. See Appendice 2. The parameter of the control law (4.8), (4.9), can be inferred from the image feature extraction of the two planes. The parameters  $e_{\theta_{s}}$  can be directly calculated from equation

4.6 and  $\mathbf{e}_{\theta_{\rm s}}$  can be indirectly computed. Also  $\theta_{\rm s}$ ,  $q_{\rm s}$  and  $q_{\rm s}^{\rm d}$  are evaluated directly from the trajectory projections. We remark that the control law (4.8), (4.9) represents a robust control, independent of the camera parameters. No intrinsec camera parameters are assumed to be known.

#### **5. Simulation**

Consider a hyperredundant manipulator that operates in OXYZ space. For simulation the following parameters will be assumed: the linear density  $\rho = 2.2$  kg/m and the length  $l = 0.6$  m. The integral differential model  $(A.1.9)$ ,  $(A.1.10)$  is simulated by using a discretization of the length with an increment  $\Delta = 0.1$ m and a discret spatial s will be s<sub>i</sub> = i · s, i=1,2..6. The MATLAB Simulink is used. The initial position of the arm is assumed to be on the OY-axis and it is defined by the two image curves,

$$
C_{s_1}^0: \quad \theta_s^0(s_i) = 0 \qquad , i=1,2..6 \tag{5.1}
$$

$$
C_{s_2}^0: \quad q_s^0(s_i^{\dagger}) = 0 \qquad \qquad j=1,2..6 \tag{5.2}
$$

The desired position is defined by the curves:

$$
C_{s_1}^d: \begin{cases} \theta_s^d(s_1) = \pi/6; \theta_s^d(s_2') = \pi/8; \theta_s^d(s_3') = \pi/10; \\ \theta_s^d(s_4') = \pi/8; \theta_s^d(s_5') = \pi/6; \theta_s^d(s_6') = \pi/4; \\ C_{s_2}^d: \begin{cases} q_s^d(s_1') = \pi/6; q_s^d(s_2') = \pi/8; q_s^d(s_3') = \pi/10; \end{cases} \end{cases}
$$
(5.3)

$$
q_s^d(s_4^{\prime}) = \pi/12; q_s^d(s_5^{\prime}) = \pi/16; q_s^d(s_6^{\prime}) = -\pi/24; \qquad \}
$$
(5.4)

The control laws (4.8), (4.9) is applied when the proportional and derivative coefficients are related as

$$
k_{\theta}^{1}(s) = k_{q}^{1}(s) = 173.6; k_{\theta}^{2}(s) = 5.6
$$
\n(5.5)



The evolution of the arm is shown in the image planes  $X_{S_1}O_{S_1}Y_{S_1}$ ,  $Z_{S_2}O_{S_2}Y_{S_2}$  (Fig. 6 and Fig.7). We remark the motion of the arm projections to the desired position by several iteration positions. By using the relations (3.9), (3.10) the angles  $\theta$  and q in 3D space are computed and the spatial arm is plotted in Fig.8. The quality of the control system can be appreciated by using the phase portrait of the evolution. The 3D error of the motion is defined by

$$
e(t) = \int_{0}^{1} ((q(s, t) - q_{d}(s)) - (\theta(s, t) - \theta_{d}(s))) \cdot ds
$$
\n(5.6)

The phase portrait is shown in Fig. 9. We remark the good stability of motion and the convergence to zero of the error.

## **6. Experimental model**

We used an experimental model presented in Fig. 10. The manipulator has a very simple design consisting of a highly elastic rod and its "backbone" with antagonic cable pairs periodically able to exert moments on the backbone to deform its shape. [1]. Although this is a truly continuous device, as a hyperredundant model, it is only actuated with 6 degrees of freedom. The driving system consists of 6 DC motors that offer the advantage of a good closed loop system. An Unversal Power Module – Quancer is used in order to implement the control of driving system. The video system is based on DT3162 frame grabber from Data Translation. Two Pulnix TMC 76S CCD cameras with Vista 4.8 mm F1.8 lens were mounted in perpendicular planes offering the input for the frame grabber. The image processing tasks are performed using Global LAB Image2 from Data Translation. The robot control algorithms are implemented in a C++ program running on a Pentium IV PC. In order to facilitate the image feature extraction, a set of markers are placed on joints along the backbone structure (Fig. 11). The localization of the markers in the image planes assures the identification of the curves  $C_{s_1}$  and  $C_{s_2}$  in the planes  $X_{S_1} O_{S_1} Y_{S_1}$  and  $Z_{S_2} O_{S_2} Y_{S_2}$  respectively. In the Fig. 12 is shown an example of curve  $C_{s_2}$  and the desired curve  $C_{s_2}^d$ .



**Figure 10** 





**Figure 11: a**)  $Z_{s_1}O_{s_2}Y_{s_2}$  image plane **b) Detail of position marker** 



**Figure 12 Postprocessed Image** 

### **7. Conclusions and Future Work**

In this paper the method of image-based servoing for a hyperredundant arm is studied. Servoing is based on binocular vision, a continuous measure of the arm parameters derrived from the real-time computation of the binocular optical flow over the two images, is compared with the desired position of the arm. The control error function is built in 3D cartesian space by the visual information obtained by two cameras in two image planes. The two 2D errors obtained in the two image planes are determined by the two differences between the actual and desired continuous angle values that define the projections of the arm shape. The plane errors can be considered as the errors of the arm shape. These errors are used to calculate the spatial error and a control law is synthesized. For the closed-loop control system and a control law the stability is proven by using the Lyapunov second method. The error function is computed in the image spaces virtually and no calibration (camera parameters) is required allowing the synthesis of more robust control laws. Future work will implement a spatial distribute observer to increase the control quality of the servoing system.

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