1. Introduction

Construction Industry Development Board (CIDB) reported that contractors waste up to 10% of the project costs when acting in a wrong way and correcting these wrong actions later. Most of construction projects involve risks that are difficult to control and analyse [1].

Contractor selection has attributes both qualitative and quantitative in nature. Construction cost and time overrun is a common problem in construction industries [2]. This is because of the sixteen following main factors: a) no clearly defined scope of project in the contract, b) no proper cost control, c) contract dispute (unclear drawings and / or guideless regulations), d) high fluctuation in commodity prices, e) the gap between construction plan and reality is too great, f) material shortage or supply delay, g) time management, h) practical experience, i) modifications of the scope of construction, j) the level of demand quality, k) project team, l) project valuation does not match the collected payment, m) procurement contract, n) geology and topography, o) climate factor, p) natural disasters.

Abbasianjahromi et al. [3] argued that present condition of the construction industry imposes onerous responsibilities on contractors so they are very eager to subcontract some of their works. Therefore, subcontracting also should to be taken into account when selecting proper construction contractor [4].

Comprehensive evaluation and proper selection of the right contractor is an important decision that has a huge impact on the overall success of a construction project. Accordingly, there is a necessity for decision support methods to assist stakeholders in making optimal decisions when selecting a contractor [5].

The standard optimisation techniques could be applied when: a) the rules of the game are well laid out; b) the environment is predictable; c) actors behaviour is deterministic; d) costs vary within a small, narrow band, and e) relationships between variables are linear.

However, deciding whether to bid on a project is commonly referred to as the bid/no-bid decision. It is a critical activity associated with complexity as well as uncertainty. Various multi-attribute decision-making methods are now available to help stakeholders in choosing the best decisive course of actions, including those for evaluation of contractors [6 – 8].
supporting products and services acquisition [9], technology [10] or software selection [11]. Some of the models that involve both monetary and non-monetary criteria can be partly considered as multi-attribute decision-making models [12 – 14], but they do not provide a mathematical formulation and an optimization model as their basis for decision-making [15]. The benefits of the above-mentioned actions in construction industry are unpredictable, relationships between attributes may be actually unknown [16]. Furthermore, modelling real-world problems with crisp values of attributes under many conditions is inadequate because human judgement and his preferences are often vague and implicit and hardly can be estimated with exact numerical values [17].

To overcome the listed shortcomings, the paper presents a novel multiple attribute Weighted Aggregated Sum Product Assessment method with the grey attributes scores – WASPAS-G method. The advantages of the proposed technique are based on its capabilities of handling imprecise information due to applied grey relations and capabilities of providing decisions of enhanced accuracy when optimizing weighted aggregated assessment. The proposed novel method is applied in a case study of evaluation and selection of a right contractor from a set of potential construction contractors.

The paper is organized as follows. Chapter 2 presents preliminaries of grey theory. The main recent applications of grey extensions of MADM (Multiple Attribute Decision Making) methods in construction engineering and management are shortly reviewed in Chapter 3. Introduction to WASPAS method and development of WASPAS-G method is presented in Chapter 4. Chapter 5 contains case study of construction contractor selection by applying the novel multiple attribute decision making method.

2. Grey Theory Preliminaries

Grey theory is a technique designed for performing prediction and decision-making in many activities. Deng [18] introduced the concepts of grey theory from a grey set by combining concepts of system theory, space theory and control theory.

Let’s start from the fact that information can be classified to three groups based on uncertainty level of initial data and named as white numbers, grey numbers and black numbers [19]. Let

\[ \otimes x = [\alpha, \beta] = x | \alpha \leq x \leq \beta, \alpha \text{ and } \beta \in R. \]  

From the above equation one can see that \( \otimes x \) consists of two real numbers: \( \alpha \) is the lower limit and \( \beta \) is the upper limit. Based on the conditions below, \( \otimes x \) can be classified as follows:

- if \( \alpha = \beta \), then \( \otimes x \) is a usual crisp number with complete information and it can be called the white number;
- else if \( \alpha \to \infty \) and \( \beta \to \infty \), then \( \otimes x \) contains no meaningful information and it can be called the black number;
- otherwise \( \otimes x = [\alpha, \beta] \) is called the grey number which means and uncertain, incomplete or insufficient information.

Usually in many cases information in real world problems is uncertain or incomplete. Consequently, extending the crisp methods with white numbers to applications with grey numbers is actually inevitable for real world decisions.

In order to apply grey arithmetic, a set of operations on grey numbers should be defined. The basic definitions and operations of two grey numbers are described as follows.

As it was described above, let a grey number to be defined by two parameters \( (\alpha, \beta) \). Let \( +, -, \times \) and \( \div \) denote the operations of addition, subtraction, multiplication and division, respectively. Some of the main operations of positive grey numbers \( \otimes n_1 \) and \( \otimes n_2 \) can be expressed as follows [20]:

Addition

\[ \otimes n_1 + \otimes n_2 = [n_{1a} + n_{2a}, n_{1b} + n_{2b}], \]  

Subtraction

\[ \otimes n_1 - \otimes n_2 = [n_{1a} - n_{2a}, n_{1b} - n_{2b}], \]  

Multiplication

\[ \otimes n_1 \times \otimes n_2 = [n_{1a} \times n_{2a}, n_{1b} \times n_{2b}], \]  

Division

\[ \otimes n_1 \div \otimes n_2 = \frac{n_{1a} \times n_{2b}}{n_{2a} \div n_{1b}} \]

only if \( n_{1a}, n_{2a}, n_{1b} \text{ and } n_{2b} \text{ does not contain 0} \)
Multiplication of grey numbers by a positive real number \( k \)

\[
k \times (n_1 \otimes n_2) = (k n_1 \otimes k n_2)
\]

Exponentiation by a natural power

\[
(n_1 \otimes n_2)^k = (n_1^k \otimes n_2^k), \quad \text{if } n_1, n_2 < 1 \text{ and } k > 1,
\]

\[
(n_1 \otimes n_2)^0 = (n_1^0 \otimes n_2^0), \quad \text{if } n_1, n_2 < 1 \text{ and } k = 0.
\]

Instead of working with an uncertain real \( x \) and applying classical arithmetic operations, a decision maker works with the grey numbers and grey arithmetic. Grey arithmetic is a powerful tool for reliable computing, and has been successfully used in the past. Recently, grey theory found a new field of applications when extending usual crisp methods, including multiple attribute decision making methods.

### 3. Recent Applications of Grey Extensions of MADM Methods

Grey theory can be successfully amalgamated with many of the decision-making processes so as to improve the quality of judgments. It is suitable for expressing quantitative but imprecise data. Also ambiguity in dealing with imprecise data can be reduced through linguistic assessment of attributes. The linguistic assessments can also be converted into associated grey values.

Below are listed some of the recent applications of interval extensions of MADM methods in civil engineering and management.

Additive Ratio ASsessment (ARAS) method with the grey attribute scores – ARAS-G, in combination with Delphi and AHP (Analytic Hierarchy Process) methods was applied by Turskis et al. [21] for improving the built and human environment through efficient decision making in renovation of urban cultural heritage. The methods enabled to combine successfully different external factors as well as stakeholders’ preferences.

Siozinyte et al. [22] applied TOPSIS-grey (Technique for Order Preference by Similarity to Ideal Solution with attributes values determined at intervals) for selecting user and environment friendly redevelopment decisions of vernacular building, involving assessment of preserved features of vernacular architecture and assuring the enforcement of contemporary building norms.

Oztaysi [23] presented selection of Content Management System among available alternatives as a multi-attribute decision making problem. A decision model built by integrating AHP and TOPSIS-grey method was proposed and applied in a foreign trade company. Besides, the effects of using different distance functions, such as Manhattan, Euclidian and Minkowski distance functions are analysed in the paper.

Zhang et al. [24] proposed an improved TOPSIS method based on weighted grey relational coefficient to evaluate and compare service quality of nine airlines and compares. The method integrates the advantage of usual TOPSIS and grey relational analysis on the curve position and the curve trend within treatment of data sequences. Authors provide a G-AHP method to determine weights, which combines the latent roots method with AHP.

Kim et al. [25] performed multi-attribute mixed type decision making by four methods, including the relative approach degree of grey TOPSIS method, the relative approach degree of grey incidence, the relative membership degree of grey incidence and the grey relation relative approach degree method using the maximum entropy estimation, respectively. In these decision making methods, the grey incidence degree in four-dimensional Euclidean space is used. The final arrangement result is obtained by weighted Borda method.

Tavana et al. [26] applied two MADM tools including fuzzy ANP (Analytic Network Process) and COPRAS-G (COmplex PRoportional Assessment) of alternatives with Grey relations, for social media platform evaluation and selection.

Nguyen et al. [27] presented hybrid approach that is also based on fuzzy ANP and COPRAS-G for multiple attribute decision making under uncertainty. Machine tools were evaluated, considering the interactions of the attributes with the help of ANP. The result is then compared with the rankings provided by other methods with grey numbers, such as TOPSIS-G, SAW-G (Simple Additive Weighting with grey numbers) and GRA (Grey Relational Analysis).

The grey-based PROMETHEE II (Preference Ranking Organization METHod for Enrichment Evaluation) methodology is designed to represent and analyse decision problems under uncertainty, which are characterized by limited
input data and uncertain preferences of decision makers. The methodology is illustrated using a case study in which source water protection strategies are ranked for Waterloo Region, Canada [28].

Stanujkic et al. [29] extended MOORA (Multi-Objective Optimization on the basis of Ratio Analysis) with performance ratings of alternatives expressed as interval grey numbers. The novel method was applied for circuit design selection in mineral processing operations. Circuit design selection was also solved by applying fuzzy MOORA [30].

It is interesting to mention that Hashemi et al. [31] extended the ELECTRE (ELimination Et Choix Traduisant la REalité, that means Elimination and Choice Expressing Reality) method with black numbers containing no meaningful information. The proposed method was applied in a supplier selection problem under ambiguous environment.

Some other extensions of crisp multiple attribute decision making methods under uncertain conditions of contractor or supplier selection are also available in recent publications. For example, Senthil et al. [32] proposed a hybrid method using AHP and fuzzy TOPSIS for contractor evaluation and selection in third-party reverse logistics. You et al. [33] proposed an extended VIKOR (VIseKriterijumska Optimizacija I Kompromisno Resenje, that means multicriteria optimization and compromise solution) method for group multi-criteria supplier selection with interval 2-tuple linguistic information. The feasibility and practicability of the proposed ITL-VIKOR method are demonstrated through three realistic supplier selection examples and comparisons with the existing approaches.

4. WASPAS-G Method

4.1 WASPAS method and its applications

Zavadskas et al. [34] proposed and originally described Weighted Aggregated Sum Product Assessment (WASPAS) method. The method aggregates the Weighted Sum Model (WSM) and the Weighted Product Model (WPM) with the help of originally derived aggregation coefficient, enabling to reach the highest accuracy of multiple attribute estimation of a problem.

There are lots of WASPAS method applications for solving MADM problems in construction. WASPAS and ARAS methods were used to evaluate potential alternatives of potential shopping mall locating by Hashemkhani Zolfani et al. [35]. Dejus and Antucheviciene [36] suggested using the WASPAS method for ranking of appropriate alternatives for occupational safety. Zavadskas et al. [37] presented an application of the method for multi-attribute assessment of public building designs alternatives, while Siozinyte and Antucheviciene [38] applied the method for assessment of windows’ design when upgrading vernacular buildings. Bagocius et al. [39] applied WASPAS method for ranking and selecting the best location for wind farms and assessing the types of wind turbines. While Vafaeipour et al. [40] used the same method of assessment in combination with Step-wise Weight Assessment Ratio Analysis (SWARA) for prioritizing regions and cities for location of solar power plants in the future. Lashgari et al. [41] applied quantitative Strategic Planning Matrix and WASPAS method that enabled to make reasoned decision in selecting the best strategies for outsourcing development. The first attempt to extend the method for problems involving uncertainty was presented as WASPAS-IVIF [42].

Based on literature review that involves development and applications mostly of a crisp method under consideration, the authors suggest that grey extension of WASPAS method is feasible for most effective real world applications. The development of a novel WASPAS-G method is presented below in the following sub-section.

4.2 WASPAS with grey values

Previously developed WASPAS method is derived on the basis of two MADM methods, i.e. WSM (Weighted Sum Model) and WPM (Weighted Product Model), aggregating them with the help of originally described optimized weighting coefficient [34].

To extend the method in vague environment with the help of grey numbers, initial decision making matrix should be presented as a grey decision-making matrix (GDMM). Matrix is composed on the basis of preferences of decision alternatives rated on attributes:
where \( m \) – number of alternatives, \( n \) – number of attributes, \( i = 1, \ldots, m \); \( j = 1, \ldots, n \); \( \otimes x_{ij} \) – denotes the grey evaluations of the \( i \)-th alternative with respect to the \( j \)-th attribute.

Next, the initial values of all the attributes should be normalized. Normalized grey evaluations of each alternative with respect to every attribute are defined as \( \otimes \tilde{x}_{ij}, i = 1, \ldots, m; j = 1, \ldots, n \), while grey initial matrix \( \otimes X \) is transformed to grey normalised decision-making matrix \( \otimes \tilde{X} \):

\[
\otimes \tilde{X} = \begin{bmatrix}
\otimes \tilde{x}_{11} & \otimes \tilde{x}_{1j} & \cdots & \otimes \tilde{x}_{1n} \\
\vdots & \ddots & \ddots & \vdots \\
\otimes \tilde{x}_{ij} & \cdots & \otimes \tilde{x}_{jj} & \cdots \\
\vdots & \ddots & \ddots & \ddots \\
\otimes \tilde{x}_{in} & \cdots & \otimes \tilde{x}_{nj} & \otimes \tilde{x}_{nn}
\end{bmatrix},
\]

As WSM and WPM methods use a linear normalization approach, corresponding values of attributes in the derivative method are also normalized by applying a linear method, adapted for grey values. Attributes with preferred maximal values are normalized as

\[
\otimes \tilde{x}_{ij} = \frac{\otimes x_{ij}}{\max_i \otimes x_{ij}}, \quad \text{i.e. } \tilde{x}_{ija} = \frac{x_{ija}}{\max_i x_{ija}}, \quad \tilde{x}_{ijb} = \frac{x_{ijb}}{\max_i x_{ijb}}.
\]

Attributes with preferred minimal values are suggested to be normalized as follows:

\[
\otimes \tilde{x}_{ij} = \frac{\min_i \otimes x_{ij}}{\otimes x_{ij}}, \quad \text{i.e. } \tilde{x}_{ija} = \frac{x_{ija}}{\min_i x_{ija}}, \quad \tilde{x}_{ijb} = \frac{x_{ijb}}{x_{ijb}}.
\]

The next task is to determine grey values of optimality functions. The grey value \( \otimes S_i \) of additive optimality function (WSM) for \( i \)-th alternative is calculated as follows:

\[\otimes S_i = \sum_{j=1}^{\min \otimes \tilde{x}_{ij}}, j = 1, \ldots, m, \text{or} \]

\[\otimes S_i = 0.5 \sum_{j=1}^{\max \otimes \tilde{x}_{ij}} \left( \tilde{x}_{ij} + \tilde{x}_{ij} \right),\]

where \( \tilde{x}_{ij} \) is normalized weighted value of the attribute. It is calculated as follows:

\[\tilde{x}_{ij} = \otimes x_{ij} \otimes w_j,\]

where \( \otimes w_j \) is the grey weight of the \( j \)-attribute and \( \otimes x_{ij} \) is the grey normalized rating of the \( i \)-th alternative with respect to the \( j \)-th attribute.

The grey value \( \otimes P_i \) of optimality function according to WPM is as follows:

\[\otimes P_i = \prod_{j=1}^{\min \otimes \tilde{x}_{ij}} \tilde{x}_{ij}^{w_j}, j = 1, \ldots, m, \text{or} \]

\[\otimes P_i = \prod_{j=1}^{\max \otimes \tilde{x}_{ij}} 0.5 \left( \tilde{x}_{ij}^{w_j} \right),\]

where \( \otimes w_j \) is the grey weight of the \( j \)-attribute and \( \otimes x_{ij} \) is the grey normalized rating of the \( i \)-th alternative with respect to the \( j \)-th attribute.

If it is proposed to determine \( \lambda \) based on assumption that total WSM grey scores should be equal to the total of WPM grey scores for all alternatives:

\[\lambda = 0.5 \sum_{j=1}^{\max \otimes \tilde{x}_{ij}} \frac{P_i}{S_j},\]

where grey values are transformed to crisp values by using the centre-of-area method, i.e.

\[\tilde{x}_{ij} = \frac{P_i + P_j}{\lambda}, \quad S_i = 0.5 \left( S_i + S_j \right)\]
The grey values of $\otimes Q_i$ can be also transformed to crisp values by the centre-of-area method.

The decreasing preference order of the alternatives is determined according to the decreasing sequence of $Q_i$.

5. Case Study of Contractor Selection

5.1 Problem formulation

Modern projects are normally characterised by huge investments, long construction periods, and complex technology. However, correlation among attributes, subjectivity of attributes weights, and heterogeneity among experts' professional capabilities for selecting contractors could not be successfully removed from the decision-making process [43]. Consequently, it is suggested that the problem be presented as GDMM and appropriate methods for evaluating and selecting contractors should also be applied.

The investing construction owner has to decide which contractors best meet his/her requirements. Based on a numerous key criteria or attributes for contractors’ evaluation that can be found in a literature [44, 45] and after interviewing purchase managers of construction companies, 6 main attributes (aggregating sub-attributes) were identified for contractor selection:

$x_1$: Bid amount. It includes four main sub-attributes (advance payment, capital bid, routine maintenance and major repairs).

$x_2$: Capability and skill, occupational health and safety. It describes contractor’s potential capacity to produce a good or service, at the same time effectively managing risk to the health and safety of his employees.

$x_3$: Technical capacity. It shows abilities to provide high quality goods, to act in the specific project and ensure future developments.

$x_4$: Managerial capability. Decision maker should be sure that the contractor would be able to manage activities, i.e. to plan, organize and control the project.

$x_5$: Past performance and experience. It includes data and opinion about the past performance of the contractor, the historical experiments of working with special projects and the amount of satisfaction or dissatisfaction. Also the attribute includes contractor’s attitudes towards continuous training and education.

$x_6$: Financial soundness. It includes four main sub-attributes as financial stability, credit rating, bank arrangement, and bonding and financial status.

Linguistic variables for grey weighting attributes are presented in Table 1. Relative importance of the listed attributes is determined by expert method. A sample of 37 experts was selected. Consistency of their ratings was found to be sufficient at a significance level = 0.05, therefore aggregated attribute weights were calculated and listed in Table 2.

Four of the possible alternatives of contractors under consideration $A_i, i = 1,…, 4$ are compared in accordance with 6 attributes and are presented in Table 3.

5.2 Results of multiple attribute analysis

The initial values of attributes were transformed to dimensionless values by applying linear normalization for grey numbers (formulae 10, 11) and processed applying the further steps of WASPAS-G method (formulae 12-17). The main stages of the solution process, including partial and final ranking of contractors are presented in Tables 4-6.

Table 1. The linguistic variables or the ratings

<table>
<thead>
<tr>
<th>Linguistic variables</th>
<th>Grey numbers</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$\alpha$</td>
</tr>
<tr>
<td>Very Low (VL)</td>
<td>0.000</td>
</tr>
<tr>
<td>Low (L)</td>
<td>0.100</td>
</tr>
<tr>
<td>Medium Low (ML)</td>
<td>0.200</td>
</tr>
<tr>
<td>Medium (M)</td>
<td>0.350</td>
</tr>
<tr>
<td>Medium High (MH)</td>
<td>0.600</td>
</tr>
<tr>
<td>High (H)</td>
<td>0.700</td>
</tr>
<tr>
<td>Very High (VH)</td>
<td>0.800</td>
</tr>
</tbody>
</table>
Table 2. The attributes for evaluation of contractors’ selection

<table>
<thead>
<tr>
<th>Attributes</th>
<th>Measure units</th>
<th>Opt.</th>
<th>Weight</th>
</tr>
</thead>
<tbody>
<tr>
<td>$x_1$ Bid amount</td>
<td>points</td>
<td>max</td>
<td>$\alpha$ 0.195 $\beta$ 0.245</td>
</tr>
<tr>
<td>$x_2$ Capability and skill</td>
<td>points</td>
<td>max</td>
<td>$\alpha$ 0.109 $\beta$ 0.129</td>
</tr>
<tr>
<td>$x_3$ Technical capacity</td>
<td>points</td>
<td>max</td>
<td>$\alpha$ 0.156 $\beta$ 0.210</td>
</tr>
<tr>
<td>$x_4$ Managerial capability</td>
<td>points</td>
<td>max</td>
<td>$\alpha$ 0.137 $\beta$ 0.182</td>
</tr>
<tr>
<td>$x_5$ Past performance and</td>
<td>points</td>
<td>max</td>
<td>$\alpha$ 0.146 $\beta$ 0.196</td>
</tr>
<tr>
<td>experience</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$x_6$ Financial soundness</td>
<td>points</td>
<td>max</td>
<td>$\alpha$ 0.137 $\beta$ 0.158</td>
</tr>
</tbody>
</table>

Table 3. Initial grey decision making matrix

<table>
<thead>
<tr>
<th>$\otimes x_1$</th>
<th>$\otimes x_2$</th>
<th>$\otimes x_3$</th>
<th>$\otimes x_4$</th>
<th>$\otimes x_5$</th>
<th>$\otimes x_6$</th>
<th>$P_i$</th>
<th>Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>$w$</td>
<td>0.195</td>
<td>0.245</td>
<td>0.109</td>
<td>0.129</td>
<td>0.156</td>
<td>0.210</td>
<td>0.137</td>
</tr>
<tr>
<td>$A_1$</td>
<td>0.632</td>
<td>0.867</td>
<td>0.470</td>
<td>0.600</td>
<td>0.663</td>
<td>0.810</td>
<td>0.430</td>
</tr>
<tr>
<td>$A_2$</td>
<td>0.532</td>
<td>0.773</td>
<td>0.750</td>
<td>0.875</td>
<td>0.512</td>
<td>0.740</td>
<td>0.340</td>
</tr>
<tr>
<td>$A_3$</td>
<td>0.507</td>
<td>0.845</td>
<td>0.550</td>
<td>0.780</td>
<td>0.659</td>
<td>0.830</td>
<td>0.550</td>
</tr>
<tr>
<td>$A_4$</td>
<td>0.725</td>
<td>0.863</td>
<td>0.670</td>
<td>0.900</td>
<td>0.709</td>
<td>0.897</td>
<td>0.320</td>
</tr>
</tbody>
</table>

Table 4. Normalised grey decision making matrix and solution results $P_i$

<table>
<thead>
<tr>
<th>$\hat{x}_1$</th>
<th>$\hat{x}_2$</th>
<th>$\hat{x}_3$</th>
<th>$\hat{x}_4$</th>
<th>$\hat{x}_5$</th>
<th>$\hat{x}_6$</th>
<th>$S_i$</th>
<th>Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_1$</td>
<td>0.100</td>
<td>0.182</td>
<td>0.057</td>
<td>0.086</td>
<td>0.115</td>
<td>0.190</td>
<td>0.113</td>
</tr>
<tr>
<td>$A_2$</td>
<td>0.084</td>
<td>0.162</td>
<td>0.091</td>
<td>0.125</td>
<td>0.089</td>
<td>0.173</td>
<td>0.090</td>
</tr>
<tr>
<td>$A_3$</td>
<td>0.080</td>
<td>0.177</td>
<td>0.067</td>
<td>0.112</td>
<td>0.115</td>
<td>0.194</td>
<td>0.145</td>
</tr>
<tr>
<td>$A_4$</td>
<td>0.115</td>
<td>0.181</td>
<td>0.081</td>
<td>0.129</td>
<td>0.123</td>
<td>0.210</td>
<td>0.084</td>
</tr>
</tbody>
</table>

Table 5. Normalised-weighted grey decision making matrix and solution results $S_i$

<table>
<thead>
<tr>
<th>$\hat{x}_1$</th>
<th>$\hat{x}_2$</th>
<th>$\hat{x}_3$</th>
<th>$\hat{x}_4$</th>
<th>$\hat{x}_5$</th>
<th>$\hat{x}_6$</th>
<th>$S_i$</th>
<th>Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_1$</td>
<td>0.100</td>
<td>0.182</td>
<td>0.057</td>
<td>0.086</td>
<td>0.115</td>
<td>0.190</td>
<td>0.113</td>
</tr>
<tr>
<td>$A_2$</td>
<td>0.084</td>
<td>0.162</td>
<td>0.091</td>
<td>0.125</td>
<td>0.089</td>
<td>0.173</td>
<td>0.090</td>
</tr>
<tr>
<td>$A_3$</td>
<td>0.080</td>
<td>0.177</td>
<td>0.067</td>
<td>0.112</td>
<td>0.115</td>
<td>0.194</td>
<td>0.145</td>
</tr>
<tr>
<td>$A_4$</td>
<td>0.115</td>
<td>0.181</td>
<td>0.081</td>
<td>0.129</td>
<td>0.123</td>
<td>0.210</td>
<td>0.084</td>
</tr>
</tbody>
</table>

Table 6. Final ranking of alternatives

<table>
<thead>
<tr>
<th>Alt.</th>
<th>$S_i$</th>
<th>$P_i$</th>
<th>$Q_i$</th>
<th>Rank</th>
</tr>
</thead>
<tbody>
<tr>
<td>$A_1$</td>
<td>0.797</td>
<td>0.670</td>
<td>0.724</td>
<td>3</td>
</tr>
<tr>
<td>$A_2$</td>
<td>0.794</td>
<td>0.670</td>
<td>0.722</td>
<td>4</td>
</tr>
<tr>
<td>$A_3$</td>
<td>0.874</td>
<td>0.747</td>
<td>0.801</td>
<td>1</td>
</tr>
<tr>
<td>$A_4$</td>
<td>0.853</td>
<td>0.717</td>
<td>0.775</td>
<td>2</td>
</tr>
<tr>
<td>$\lambda$</td>
<td>$\alpha$ 3.318</td>
<td>$\Sigma$ 2.805</td>
<td>$\lambda$ 0.423</td>
<td></td>
</tr>
</tbody>
</table>
6. Conclusions

After processing the given data on decision alternatives as well as attributes and their preferences as GDMM, rational solutions about contractor’s selection can be made even in a vague environment. Solution of the presented problem by applying a novel WASPAS-G method shows that alternatives finally ranked as follows: $A_3 > A_4 > A_1 > A_2$. While, if taken into account only additive part of the method, alternatives rank $A_3 > A_4 > A_2 > A_1$, and if taken into account only exponential part of the method, alternatives are located as follows $A_3 > A_4 > A_1 = A_2$ and the final ranking order is not clearly defined.

The proposed novel aggregated WASPAS-G method is a valuable tool for making a more precise decision, considering preferences of stakeholders in an uncertain environment.

REFERENCES


